



A kinetic model of the transformation of a micropatterned amorphous precursor into a porous single crystal

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ABSTRACT

Biogenic single crystals with complex shapes are believed to be generated by the crystallization of an amorphous precursor. Recent biomimetic experiments on the crystallization of calcite via amorphous-to-crystalline transition point to the fact that the transformation kinetics may be controlled by the micropattern and the macroscopic shape of the amorphous precursor phase. Here we analyse a simple kinetic model, based on thermodynamic considerations, showing that the presence of cavities in the micropatterned precursor phase might interfere with the transformation process and control its kinetics. The size of the cavities couples to the total surface energy and, hence, to crystal nucleation and growth, while the spacing of the cavities, as compared to the typical diffusion path, controls the possible nucleation of competing crystals.

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1. Introduction

Many biological crystals are grown by the transformation of amorphous precursor phases [1–8]. For example, it has been shown that amorphous calcium carbonate (ACC) transforms into calcite or aragonite in the skeletons of echinoderms and molluscs, and that amorphous iron oxides transform into magnetite in chiton teeth. The advantage of this type of processing is that it apparently allows the growth of single crystals with very complex shapes [9,10]. It has also been argued that amorphous precursor phases substantially modify the nucleation process as several subcritical nuclei may coexist, survive and eventually coalesce within a single amorphous precursor particle [11–17]. Recently, it has become possible to stabilize amorphous calcium carbonate as a precursor of calcite crystals in laboratory conditions and to initiate controlled crystallization of large single crystals [17–21].

One of the challenges in understanding the kinetics of this transformation is to rationalize the effect of the volume change between ACC and calcite, which is much denser. Hence, crystallization of ACC is not possible without considerable mass transport at the nano- and micrometer levels. It is quite surprising that the formation of a large single crystal is actually possible under these conditions.

One would suspect that the negative volume jump from ACC to calcite would disrupt the crystallization front and the remaining ACC pool, making the growth of a single crystal difficult. Indeed, the formation of polycrystalline calcite is observed when a large plate-like ACC template transforms, even starting from a single artificial nucleation site [18]. However, when the ACC template is pre-structured by a periodic array of holes (cavities) in the plate-like template, a large single crystal may grow under similar conditions [18,22]. As shown in Fig. 1, large single crystals with periodic arrays of holes occur in natural systems and can be grown in the laboratory. The size and spacing of these holes seem to play a major role in the kinetics of the crystallization process, since a single crystal is formed only when the spacing of the holes is sufficiently small. The size of the holes has been observed to increase during crystallization, clearly compensating for the volume decrease from ACC to calcite. All these experimental observations suggest an important role of geometric constraints in the transformation process from an amorphous precursor to a single crystal, but the physical nature of this influence is still uncertain.

2. Problem formulation

In this paper, we carry out theoretical investigations of the influence of geometric constraints on a phase transformation process with a considerable volume jump. The hypothesis that cavities in the precursor reduce the mechanical stresses arising from the

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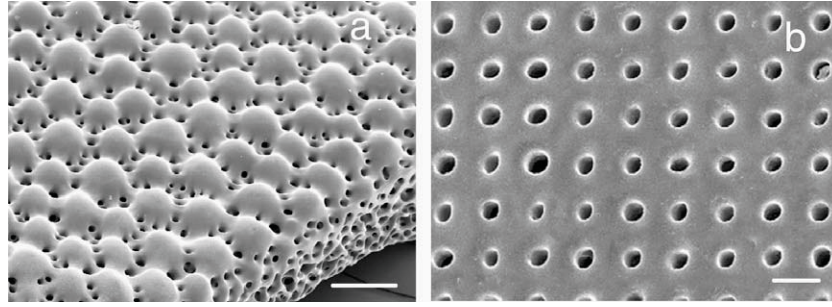


Fig. 1. (a) Scanning electron micrograph (SEM) of a part of the skeleton of a brittlestar *Ophiocoma wendtii* (Ophioroidea, Echinodermata). The entire structure (the mesh and the array of microlenses) is composed of a single calcite crystal used by the organism for mechanical and optical functions [9]. (b) SEM of a sample micropatterned single calcite crystal fabricated by transformation of an amorphous precursor. The holes were pre-existing in the precursor and grew during the transformation process [18]. Bar = 100 and 10 μm in (a) and (b), respectively.

volume change [18] is not likely to be true, because the presence of holes leads to stress concentration and increases the risk of failure initiation, rather than preventing the disruption between the parent ACC phase and the crystal [23]. To avoid this, the parent phase has to be sufficiently ductile to allow for accommodation of the deformation without stress concentrations. The latter condition is fulfilled for the water-rich ACC phase, which is quite soft and deformable compared to calcite. Moreover, recent experiments on the controlled crystallization of ACC show that, indeed, ACC rearranges considerably around growing crystals to form halos [19].

Here we analyse the possible influence of holes on the kinetics of the transformation of ACC to calcite within a simple theoretical model. We find that the presence of cavities in the micron range can inhibit calcite nucleation and promote the growth of a single crystal from a sufficiently large artificial nucleus. We show that the time required for the crystal surface to bridge the distance a between two holes scales as a^2 , which needs to be compared to the time for nucleation of a competing crystal. Hence, a single-domain crystal will only form when the distance between holes is small enough to prevent secondary nucleation.

The model studied is (quasi-) two-dimensional, consisting of a planar, perforated layer (with a large thickness d) of ACC with the starting configuration shown in Fig. 2. The ACC layer contains a periodic array of circular holes with radius ρ_w and the initial ra-

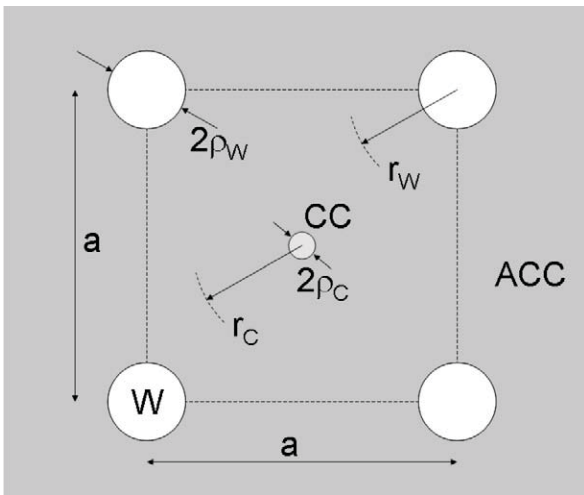


Fig. 2. Sketch of the configuration of holes (W) and the calcite nucleus (CC) in the ACC plate. The holes with radius ρ_w (with ρ_{w0} being its initial value at the start of crystallization) are arranged on a square lattice with spacing a . The radius of the calcite nucleus is ρ_c , and the distance from the centre of the calcite nucleus and of the holes is r_c and r_w , respectively.

dius ρ_{w0} , distributed in a square lattice with the unit cell dimension of a . During a diffusive transformation process the phase ACC transforms into crystalline calcite (CC) and liquid water (W). The molar fractions, molar volumes and molar Gibbs energies of individual phases are listed in Table 1.

3. Problem solution

We assume that, at the beginning of the phase transformation, a calcite nucleus grows to an initially very small circle around the centre with radius ρ_c , while the holes increase their radius from ρ_{w0} to ρ_w in order to compensate for the decrease of the volume of calcium carbonate during the transformation from the ACC to the calcite phase. We postulate that the accommodation of the transformation strain, arising from significant shrinking, can be realized by the viscous behaviour of the ACC. Without this property of the ACC, transformation stresses would accumulate at the interface between calcite and ACC, which must lead either to a stopping of the transformation or to a fracture of the specimen.

When the calcite crystal grows from 0 to ρ_c and the holes grow from ρ_{w0} to ρ_w , we can write two conservation relations – one for the calcite and one for the water.

The first one expresses the conservation of calcium ions, with x being the molar fraction of water in ACC:

$$\frac{M_C}{d} = \frac{\pi \rho_c^2}{\Omega_C} = (1-x) \frac{M_A}{d} = (1-x) \frac{\pi \rho_c^2 + \pi \rho_w^2 - \pi \rho_{w0}^2}{\Omega_A}, \quad (1)$$

where it is assumed that M_A moles of the amorphous phase is being transformed into M_C moles of calcite and that the layer thickness d remains roughly unchanged during the crystallization (that is, the mass redistribution is supposed to mainly occur within the plane of the layer and not in the third dimension). This equation can be transformed to

$$\frac{\rho_w^2 - \rho_{w0}^2}{\rho_c^2} = \frac{\Omega_A}{(1-x)\Omega_C} - 1 \equiv \alpha, \quad (2)$$

where the parameter α describes the relative volume decrease when a given amount of calcium atoms transforms from ACC to calcite. The quantities Ω_A and Ω_C are the molar volumes of ACC and calcite (see Table 1).

The second conservation relation defines the total number M_W of moles of water which had to leave the amorphous phase during the transformation process:

$$\frac{M_W}{d} = x \frac{M_A}{d} = \frac{x}{1-x} \frac{\pi \rho_c^2}{\Omega_C}. \quad (3)$$

The change ΔG in the total Gibbs free energy G (within the unit cell in Fig. 2) due to the nucleation of a calcite crystal of size ρ_c is given

Table 1

Definition of thermodynamic quantities for the different phases (columns 2–4) and of the interfaces between water and ACC and between calcite and ACC (last two columns).

Phase	Bulk properties			Interface properties	
	Molar fraction H ₂ O	Molar volume (m ³ mol ⁻¹)	Molar Gibbs energy (J mol ⁻¹)	Interface energy (J m ⁻²)	Radius (m)
Water	1	Ω_W	g_W	γ_W	ρ_W
ACC	x	$\Omega_A(x)$	g_A		
Calcite	0	Ω_C	g_C	γ_C	ρ_C

by a sum of the contributions from the bulk phases and from their respective interfaces as

$$\Delta G = -M_A g_A + M_C g_C + M_W g_W + 2\pi d(\rho_C \gamma_C + (\rho_W - \rho_{W0}) \gamma_W) \quad (4)$$

(for definitions see Table 1). Using relations (1)–(3), we can eliminate ρ_W in the expression for ΔG and obtain:

$$\Delta G/d = -\pi \rho_C^2 \hat{g} + 2\pi (\gamma_C \rho_C + \gamma_W (\sqrt{\rho_{W0}^2 + \alpha \rho_C^2} - \rho_{W0})), \quad (5)$$

$$\hat{g} = \frac{g_A - (1-x)g_C - xg_W}{(1-x)\Omega_C} \geq 0.$$

The expression \hat{g} corresponds to the decrease in molar Gibbs energy during the transformation. The energy difference $\Delta G/d$ must be positive to allow for crystallization. This expression neglects the change of the ACC–water interface into a calcite–water interface on the upper and lower sides of the slab. Taking this contribution into account, \hat{g} would have to be replaced by $\hat{g} + 2(\gamma_W - \gamma'_W)/d$, where γ'_W is the surface energy of the calcite–water interface. We estimate \hat{g} to be in the order of $1.3 \times 10^8 \text{ J m}^{-3}$ [24]. This value is obtained by using the following thermodynamic values reported for calcite and the hydrated calcium carbonate mineral monohydrocalcite (as we do not have good thermodynamic data for the hydrated ACC): $g_A/(1-x) = -1537 \text{ kJ/mol}$ and $x = 1/2$ for monohydrocalcite, $g_C = -1235 \text{ kJ/mol}$ for calcite, $g_W = -307 \text{ kJ/mol}$ for water at 25 °C [24] and $\Omega_C = 3.69 \times 10^{-5} \text{ m}^3/\text{mol}$. (Note that, taking ikaite instead of monohydrocalcite for this estimate, one would find \hat{g} to be in the order of $3 \times 10^8 \text{ J m}^{-3}$). We do not have good data for γ'_W , but the calcite–water interface energy has been reported to be of the order of $\gamma'_W = 0.1 \text{ J m}^{-2}$ [25]. Taking $\gamma_W - \gamma'_W$ to be of the same order, then $2(\gamma_W - \gamma'_W)/d$ will be much smaller than \hat{g} for layer thicknesses in the micron or millimetre range. It is therefore sufficient to consider \hat{g} in Eq. (5).

The analysis of this expression (5) also suggests that the presence of the holes adds surface energy (which depends differently on ρ_C than the \hat{g} term) to the system and therefore reduces the growth rate of a nucleus. The calcite nucleus will grow if its radius is larger than the value of ρ_C that minimizes ΔG . To get a simple understanding of Eq. (5), we first assume that the interface energy between calcite and ACC is much lower than that between ACC and water and, if we set γ_C to zero in the derivative of Eq. (5) with respect to ρ_C , one finds that the calcite nucleus can grow if

$$\rho_{W0}^2 + \alpha \rho_C^2 \geq (\alpha \gamma_W / \hat{g})^2 = \tilde{\rho}^2. \quad (6)$$

As a consequence, an initial hole that is large enough (the critical value being $\rho_{W0} > \tilde{\rho}$) does not hinder the growth of the calcite nucleus. In order to get a first approximation for ρ_{W0} , we take $\gamma_W \approx 0.1 \text{ J m}^{-2}$ and $\hat{g} \approx 1.3 \times 10^8 \text{ J m}^{-3}$. With the volume increase α being of the order of 1 ($\alpha = 0.33$ for monohydrocalcite and $\alpha = 2$ for ikaite), the order of magnitude for $\tilde{\rho}$ is then about 1 nm. This is quite small and, under such circumstances, the initial hole will not change the growth behaviour of the calcite nucleus. The situation would, however, be completely different in a setting where the ACC were stabilized (e.g. by some additive) so that the driving force for crystallization, \hat{g} , would be reduced to, say, 10^6 J m^{-3} or less. Then the critical size for the initial hole would be of the order of microm-

eters and the growth of the calcite nucleus would be strongly influenced by the presence of the holes.

One may imagine two scenarios:

- (1) $\rho_{W0} > \tilde{\rho}$: under these conditions, the initial holes in the ACC layer do not essentially influence the growth of the calcite nucleus (except for a slight reduction of the driving force \hat{g}).
- (2) $\rho_{W0} < \tilde{\rho}$: under these conditions, the holes in the structure are hindering the growth of calcite nuclei smaller than $\sqrt{(\tilde{\rho}^2 - \rho_{W0}^2)/\alpha}$. Typically this value will be of the same order of magnitude as $\tilde{\rho}$, which means that calcite nucleation will effectively be suppressed if $\tilde{\rho}$ is of the order of micrometers. Starting from a single (sufficiently large) nucleus, this situation might favour the growth of a single crystal during the crystallization of ACC.

To obtain some information about the transformation kinetics, one needs to consider that water must be transported by diffusion in ACC from the site where calcite transformation occurs to the interfaces. This is sketched in Fig. 3. Depending on the distance of the transformation front to the nearest hole in relation to the slab thickness, the water flux will be predominantly to the hole or to the surface above and below. Viscous flow then drives the calcium carbonate in the opposite direction. Typically, the calcite crystal grows until all the calcium carbonate present in the near neighbourhood has been consumed. For isolated nuclei, this apparently leads to circular regions around each calcite crystal where ACC has been depleted [19]. In particular, if there are no holes in the structure, exchange is only possible with the upper and lower surface. However, if the a/d ratio is small enough, diffusion will be mostly in-plane, transporting water from the transformation front into the hole. This is the situation considered in our model.

Assuming that there is a simplified field of diffusive flux of water consisting of two overlapping radial fields (see Fig. 2), and that there is no water in the calcite phase and no water at the hole interface (water is getting out of the solid phase at the hole), we can derive simple solutions for the fluxes in terms of 1/distance (specifically, see e.g. Section 3 of Ref. [26]):

$$j_C = \dot{\rho}_C \frac{x}{\Omega_A} \frac{\rho_C}{r_C} \quad \text{and} \quad j_W = \dot{\rho}_W \frac{x}{\Omega_A} \frac{\rho_W}{r_W}. \quad (7)$$

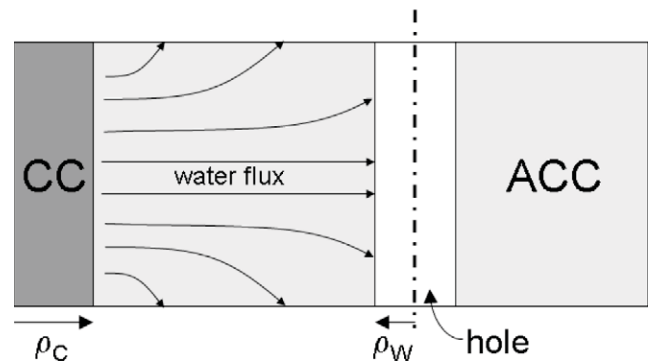


Fig. 3. Water flux from the transformation front to the specimen surface.

With these fluxes, we can calculate the total energy dissipation from diffusion (according to Section 3 and Appendix B of Ref. [27]) as

$$Q/d = \int_{\rho_c}^{a/2} \frac{j_c^2}{A_c} 2\pi r_c dr_c + \int_{\rho_w}^{a/2} \frac{j_w^2}{A_w} 2\pi r_w dr_w, \quad \text{with}$$

$$A_c = A_w = \frac{x D_w}{\Omega_A R_g T}, \quad (8)$$

where R_g is the gas constant, T is the temperature, D_w is the diffusion coefficient of water in ACC, and the quantities A_c and A_w are the “bulk” mobilities of water. Using Eq. (2) in rate form, $\rho_w \dot{\rho}_w = \alpha \rho_c \dot{\rho}_c$, the abbreviations $y = 2 \rho_c / a$ and $\beta = 2 \rho_{w0} / a$, and a renormalized time $\tau = D_w t / a^2$, we get:

$$Q/d = -\frac{\pi x R_g T D_w}{16 \Omega_A} \dot{y}^2 y^2 (2 \ln y + \alpha^2 \ln(\beta^2 + \alpha y^2)), \quad (9)$$

where $\dot{y} = dy/d\tau$. The kinetics of a system follows from Onsager's principle of maximizing the dissipation Q with the boundary condition $Q = -\dot{G} = -\Delta \dot{G}$ (for details on this principle, see Ref. [28], and for applications on diffusion problems, see Ref. [27] and later Ref. [29]). In the case at hand, for a fixed value of α we have only one internal variable describing the system, namely ρ_c , and its rate $\dot{\rho}_c$, which can immediately be found by equating $-\dot{G}$ from Eq. (5) with Q from Eq. (9). Neglecting the contribution from the surfaces at sufficiently large times, we arrive at: $-\dot{G}/d = \pi D_w y \dot{y} \hat{g}/2$. Equating this with Eq. (9) leads to a differential equation in y which can be analytically integrated to give:

$$K\tau = (1 + \alpha^2)y^2 + \alpha\beta^2 \ln \beta^2 - [y^2 \ln y^2 + \alpha(\beta^2 + \alpha y^2) \ln(\beta^2 + \alpha y^2)], \quad (10)$$

where $K = 16 \Omega_A \hat{g} / (x R_g T)$ is a dimensionless constant. Fig. 4 shows graphs of the function $y(\tau)$ for various values of the parameters α and β .

It is apparent from the growth kinetics shown in Fig. 4 that, at fixed parameters α and β , the time for the crystal to grow towards the next hole scales with a^2 and is not linear in a . As a consequence, we expect that, if the distance between holes becomes too large, the time for the single crystal to grow becomes large compared to the time needed for the nucleation of other crystals. If the first crystal has grown to the neighbouring hole, the model can be applied again, with the nucleus now being at the advancing crystal front. Therefore, the time for the crystal to grow over many holes will scale linearly (not quadratically) with the number of holes.

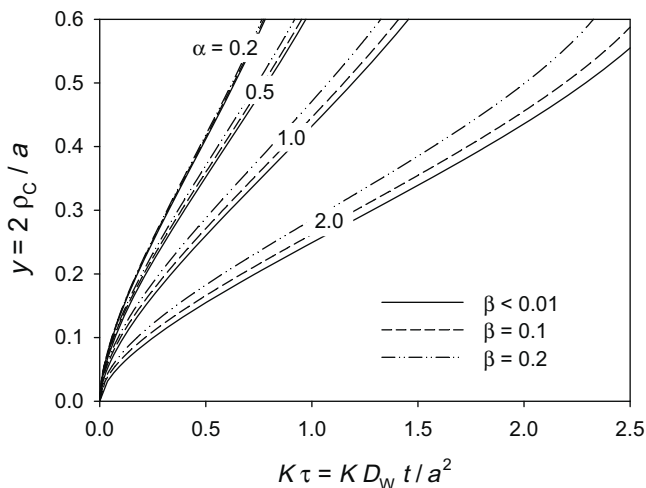


Fig. 4. Plots of the nucleus diameter normalized by the lattice spacing, y , as a function of normalized time K for several values of the relative volume jump, α , and the initial hole diameter relative to the lattice spacing, β , according to Eq. (10).

The dependence on the initial size of the holes (that is, on the dimensionless parameter β) is weak (see Fig. 4) as long as it is large enough to overcome the surface tension (see the discussion after Eq. (6)). The dependence on the volume jump α from ACC to calcite is, however, important, with considerable retardation of the crystallization when α gets larger.

4. Discussion and conclusion

Our theoretical analysis of the transformation process of the micropatterned ACC to calcite shows that the existence of cavities in a slab-like amorphous precursor has several profound consequences for the crystallization kinetics:

- (1) The cavities may act as a sink for water to compensate for the volume change during the crystallization of ACC into calcite. This requires, however, that the thickness d of the precursor slab should not be much smaller than the spacing between cavities, so that a/d should be in the order of unity or less.
- (2) In addition, small cavities hinder the growth of calcite nuclei. In particular, if the driving force for crystallization is small enough and the size of the cavities are below a critical threshold, the nucleation of calcite is suppressed, and only one large nucleus may grow (eventually into a single crystal).
- (3) The transformation time scales with a^2 and the calcite crystal nucleus grows to a given size roughly as the square root of time. This means that for large values of a the nucleation rate of competing crystals from the same precursor might also prevent the growth of a single crystal, even if condition 2 is fulfilled.

These mechanistic considerations are not only in agreement with the existing experimental data [18], but also add a higher level of understanding of the crystallization process. Indeed, for a slab thickness d of 10 μm and a spacing a between holes in the same order, the formation of a single crystal from a single nucleus has been found experimentally (Fig. 1). When the spacing a was increased to 100 μm , however, polycrystalline calcite appeared [18] (in agreement with the fact that $a/d \gg 1$). The fact that the transformation starts and progresses from a single nucleation site indicates that heterogeneous nucleation is rather low (except at the artificial nucleus) in this system. This fact justifies the current modelling approach, which would not be valid in a situation where heterogeneous nucleation (e.g. at walls or surfaces) dominates. In particular, the above analysis confirms the importance of geometric constraints on the transformation kinetics and enables a rational design of the crystallization environment and space. It provides the absolute value of the cavity spacing a , of its ratio to the slab thickness d and of the cavity size required to optimize the probability for the growth of a large single crystal from an amorphous precursor. Using these parameters, one can generate artificial crystals of arbitrary shapes similar to the convoluted micropatterns of their biogenic single-crystalline counterparts. However, one should be quite careful in extrapolating these considerations to single crystal formation in biological organisms, where the amorphous precursor phase is often anhydrous [8]. In such situations, water diffusion cannot be the controlling mechanism, but it is not unlikely that the diffusion of other ions or molecules stabilizing the precursor phase [30] could play a similar role.

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